

# CS 526

# A Advanced

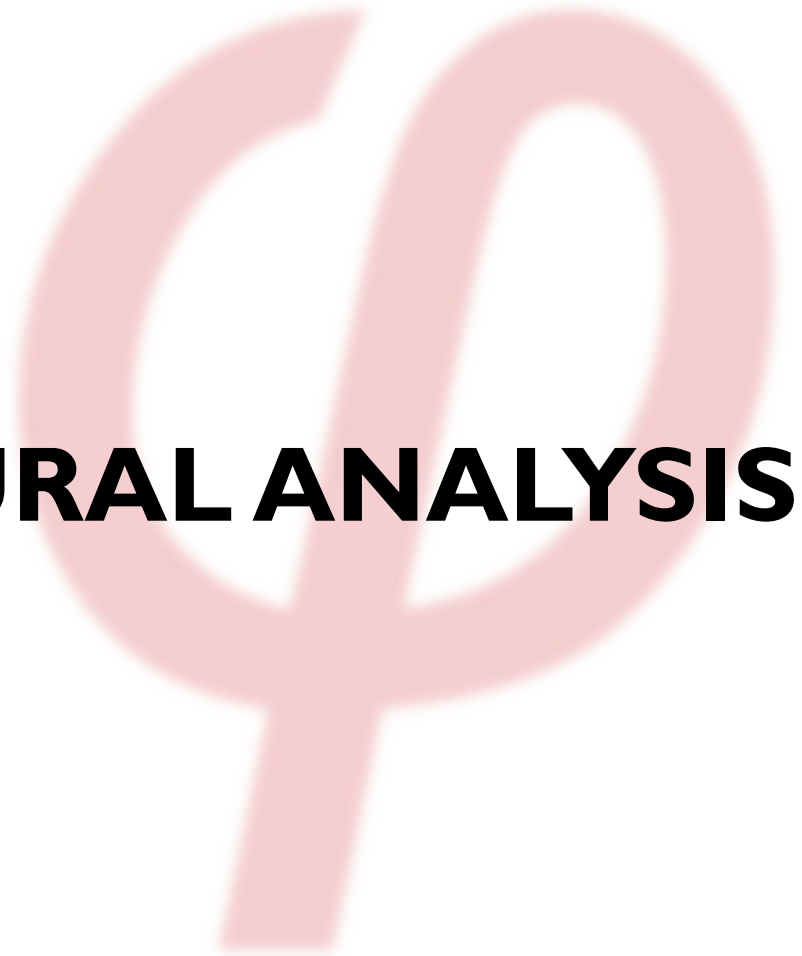
# C Compiler

# C Construction

<https://charithm.web.illinois.edu/cs526/sp2022/>  
(slides adapted from Sasa and Vikram)

# **INTERPROCEDURAL ANALYSIS**

The slides adapted from Vikram Adve



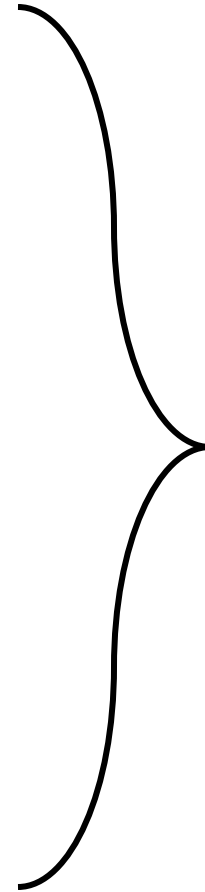
# So Far...

Control Flow Analysis

Data Flow Analysis

Dependence Analysis

Points-to Analysis



**All within  
a single  
procedure  
(intraprocedural)**

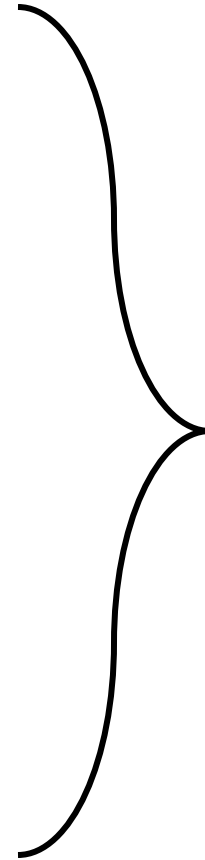
# Today

Control Flow Analysis

Data Flow Analysis

Dependence Analysis

Points-to Analysis



**Across  
multiple  
procedures  
(interprocedural)**

# Today

## Control Flow Analysis



**Key question to answer:**

**How to deal with function call  $y = f(x)$ ?**

**(we will describe this for a subset of techniques)**

# Why interprocedural analysis and optimization?

- **Produce better code around call sites**  
avoid saves, restores; understand cross-call site data flow
- **Produce tailored copies of procedures**  
often, full generality is not necessary;  
constant valued parameters, aliases
- **Provide sharper global (*intraprocedural*) analysis**  
improve on conservative assumptions  
especially true for global variables
- **Present the optimizer with more context**  
languages with short procedures; assumes context  
improves code

# Key Challenges

## Compilation Time, Memory

Key problem: scalability to large programs

- Dominated by analysis time/memory
- Flow-sensitive analyses: bottleneck often memory (!time)
- $\Rightarrow$  Often limited to fast but imprecise analyses

## Multiple calling environments

Different calls to  $P()$  have different properties:

- known constants, aliases, surrounding execution context (e.g., enclosing loops), function-pointer arguments, ...
- frequency of the call

# Key Challenges

## Recursion

Recursive codes are typically like most difficult types of loops

- No induction variables, complex data structures, complex termination

## Estimating profitability

- even inlining is not clear win
- separation of concerns:
  - ignores resource constraints
  - works best with smaller procedures



# Solution #1:

## Reduction to Intraprocedural

### 1. Conservative:

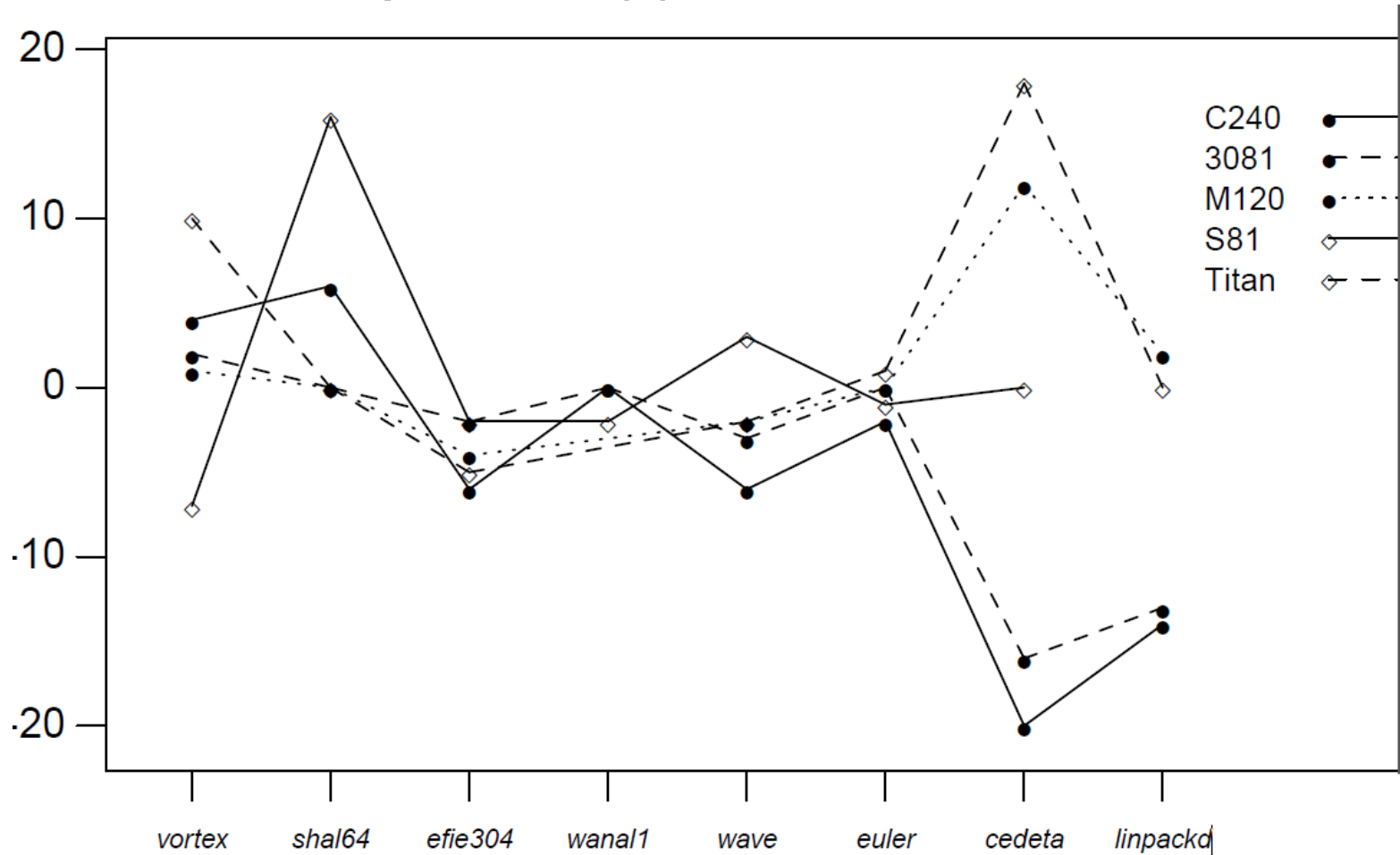
- Analyze each function separately
- At every function call, invalidate all global variables
- The result for each function is conservative, for all values of the input variables

### 2. Inlining:

- At each call, insert the function body
- Can optimize better, use local values of variables
- However, the control flow graph grows exponentially
- Also, recursion causes problems

# Inlining Benefits

↓ Performance Improvement (%)



## **Solution #2:**

# **Analyze Global Flows**

## **Create Whole-Program CFG**

- Possible unrealizable paths
- Tradeoff between precision and space

## **Call String Approach**

- Maintain the context of caller, each call site can have a different analysis
- Call context simulates stack
- Finite unrolling for recursion

# Realizable Paths

## Definition: Realizable Path

A program path is realizable iff every procedure call on the path returns control to the point where it was called (or to a legal exception handler or program exit)

## Whole-program Control Flow Graph?

Conceptually extend CFG to span whole program:

- split a call node in CFG into two nodes: CALL and RETURN
- add edge from CALL to ENTRY node of each callee
- add edge from EXIT node of each callee to RETURN

Problem: This produces many unrealizable paths

Focusing only on **realizable paths** requires **context-sensitive analysis**

# MOP and MVP Solutions

Previously, we learned about meet-over-paths (MOP) solutions for dataflow equations

- These were desired solutions of the analysis

For interprocedural analysis, we need to define a new **meet-over-valid-paths (MVP)** solution, which only *combines dataflow facts over the realizable paths*.

- Avoids the paths induced by conservative whole-program CFG.
- These would be the desired solutions of interprocedural problems

# Call Graph

## Call Graph:

- represents how the procedures (subprograms) are being called within the program code
- Nodes represent procedures, e.g.,  $f$ ,  $g$ ...
- Edges  $(f, g)$  specify the caller and the callee, e.g., procedure  $f$  calls procedure  $g$ .
- A cycle in the graph indicates recursive procedure calls

# Building the Call Graph

**Function pointer variables make this problem hard!**

Fortran: only formal arguments (no assignment)

C, C++, Java, ...: arbitrary function pointer variables and uses

```
void main () {  
    confuse(a,c)  
    confuse(b,d)  
}
```

```
void confuse(fptr1 x, fptr0 y) { (*x)(y) }
```

```
void a(fptr0 z) { (*z)() }
```

```
void b(fptr0 z) { (*z)() }
```

```
void c { ... }
```

```
void d { ... }
```

# Languages with **Function Pointer** Assignment

## **Approach 1: Solve CALLS and ALIAS separately**

- Compute whole-program call graph
- Solve ALIAS
- Refine call graph

(Iterate ALIAS and CALLS until there are no changes)

## **Approach 2: Solve CALLS and ALIAS simultaneously**

Context-sensitive alias analysis algorithms can discover call graph as they propagate points-to sets:

- Liang and Harrold (FSE 1999)
- Fähndrich, Rehof and Das (PLDI 2000)
- Lattner and Adve (PLDI 2007)



# Call Graph: Previous Results

## Fortran with Recursion

Precise graph: Callahan, Carle, Hall, Kennedy (87, 90)

- $O(N^{v_{\max}+1})$  logical steps  $N = \#$ procedures  
 $v_{\max} = \max.$  #procedure-valued parameters for any procedure

Conservative, approximate graph: Hall, Kennedy (90)

- $O(N + PE)$  logical steps  $P = \#$ procedures passed as parameters

## Object-oriented Languages

A framework for call graph construction algorithms, David Grove, Craig Chambers. *ACM TOPLAS*, 23(6), November 2001

- Describes several alternative algorithms in a common framework
- Incorporates class hierarchy analysis, MOD, exception analysis, escape analysis

## Solution #3:

# Functional Approach

**Previous:** Saves space, but still iterates many times of the function

**Goal:** Establish the input/output relationship for the function, i.e., compute function summary

- Analyze once, compute function summary
- At call sites, specialize this summary, without looking at the body
- For recursive calls, unroll

# Classification of IP\* Analyses

**Flow-insensitive:** computes a single result for entire program/procedure

- Can be solved in time polynomial in the size of the call graph (Banning, POPL, 1979)

**Flow-sensitive:** computes distinct result for each program point

- NP-complete or Co-NP complete (Myers, POPL, 1981).

**Context-insensitive:** includes realizable and unrealizable paths

**Context-sensitive:** explicitly excludes unrealizable paths

**May problems** describe events that may happen as the result of executing a given call

**Must problems** describe events that always happen when a given call is executed

# Classical IP problems

**Side-effect problems:** “backward” IP dataflow problems

**Propagation problems:** “forward” IP dataflow problems

(where backward and forward refer to call-graph).

- **CALLS:** Constructing the call graph
- **ALIAS:** Alias analysis
- **MOD:** Variables possibly modified due to a call
- **REF:** Variables possibly used due to a call
- **KILL:** Variables definitely modified before use due to a call
- **USE:** Variables possibly used before being modified due to a call
- **CONST:** Constant propagation

# IP Constant Propagation

## The problem

Compute sets of pairs  $(name, value)$  at entry to each function and after each call site, where  $value$  is an element of the usual CONST lattice (T,  $\perp$ , or constant value).

## Key considerations

1. Constant values available at call sites
  - deriving initial information
2. Transmission of values across call sites and returns
  - interprocedural data-flow problem
3. Transmission of values through procedure bodies
  - single procedure data flow (*jump function*)

# IP Constant Propagation

## Build interprocedural value graph

- analogous to the SSA graph used in SCCP
- standard CONST lattice: values are either T, (constant), or  $\perp$

## Use a standard iterative approach:

- maintain a worklist of formal parameters
- add a parameter to the worklist every time it changes value
- any parameter changes value at most twice

# IP Constant Propagation

## Challenges:

1. Overall problem is undecidable.
2. Constant propagation is flow-sensitive:  
⇒ Must have all procedures in memory simultaneously

**Solution:** Capture approximate effects of function bodies with “**jump functions**.”

Callahan, Cooper, Kennedy, and Torczon, “Interprocedural constant propagation”, SIGPLAN 86, July 1986.

Interprocedural Constant Propagation: A Study of Jump Function Implementations, Dan Grove and Linda Torczon. PLDI 1993.

# IP Constant Propagation

Use two types of jump functions:

- **forward jump function:** value passed to a formal parameter at a call-site (as function of formal parameters of caller)
- **return jump function:** each return value from a procedure (as a function of formal parameters of the procedure)

For a procedure  $p$  we define  $J_s^y$  - for an actual parameter  $y$  gives the expression of  $p$ 's formal arguments at the call site  $s$



# Example Jump Functions

## Literal Constant Jump Function:

$J_s^y = c$ , if  $y$  is the literal constant  $c$  at call site  $s$  (else,  $\perp$ )

## Intraprocedural Constant Jump Function:

$J_s^y = c$ , if intraprocedural analysis or value numbering can prove  $y = c$  at the call site  $s$  (else,  $\perp$ )

## Pass-through Parameter Jump Function:

$J_s^y = c$ , (as above), or  
 $x$ , if  $y = x$  at  $s$  and  $x$  is a formal parameter of the calling procedure (else,  $\perp$ )

## Polynomial Parameter Jump Function:

$J_s^y = c$  (as above), or  
 $f(\vec{x})$  if  $y = f(\vec{x})$  at  $s$ , where  $\vec{x}$  are formal parameters of the calling procedure and  $f$  is a polynomial function (else,  $\perp$ )

# Constants found through the use of jump functions

<i>Program</i>	<i>Using Return Jump Functions</i>				<i>No Return Jump Functions</i>	
	Polynomial	Pass-through	Intraprocedural	Literal	Polynomial	Pass through
adm	110	110	110	110	110	110
doduc	289	289	289	288	287	287
fpppp	60	60	54	49	56	56
linpackd	170	170	170	94	170	170
matrix300	138	138	122	71	138	138
mdg	41	41	40	31	40	40
ocean	194	194	194	57	62	62
qcd	180	180	180	180	180	180
simple	183	183	179	174	183	183
snasa7	336	336	336	254	336	336
spec77	137	137	137	104	137	137
trfd	16	16	16	16	16	16

Interprocedural Constant Propagation: A Study of Jump Function Implementations, Dan Grove and Linda Torczon. PLDI 1993.

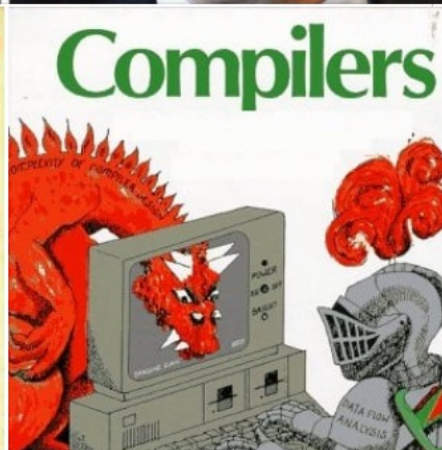
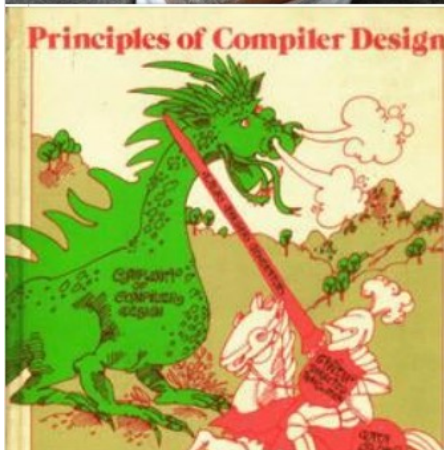


Saman Amarasinghe

23h · 🌐



Compilers rock!! **Congratulations!!!**



**CSAIL - MIT**

Yesterday at 8:20 AM · 🌐

**BREAKING:** This year's \$1 million Turing Award - often described as "the Nobel Prize for computing" - goes to Jeffrey Ullman & Alfred Aho for their work in compilers.

They co-wrote 2 classic computer science texts: the green and red "dragon books" (1977 & 1986).

More info: <https://www.cnet.com/.../turing-award-goes-to.../>

# Interprocedural Side-Effect Problems

“A Schema for Interprocedural Modification Side-Effect Analysis with Pointer Aliasing,” W. Landi et al., ACM TOPLAS, March 2001.

**Problems** (for a call site  $s: y = f(x_1 \dots x_n)$  )

- **MOD(s):**  
 $v \in \text{MOD}(s)$  iff statement  $s$  may change value of variable  $v$
- **MOD(F):**  
 $v \in \text{MOD}(F)$  iff function  $F$  may change value of variable  $v$
- Similarly **REF(s), REF(F):**  
 $v \in \text{REF}(*)$  iff statement/function might reference  $v$ 's value

# Interprocedural Side-Effect Analysis

**Compute:**  $\text{MOD}(s)$ ,  $\text{MOD}(F)$ ,  $\text{REF}(s)$ ,  $\text{REF}(F)$

## Strategy

1. Perform interprocedural alias analysis (perhaps context-sensitive)
2. Compute direct side-effects of assignments
3. Solve dataflow equations iteratively on the Interprocedural Control Flow Graph
  - Use context in each dataflow equation
  - Here context captured by reaching aliases – **RAs**  
(see: Landi and Ryder. A safe approximation algorithm for interprocedural pointer aliasing. PLDI 1992)

# Reaching Alias

The data-flow fact that  $x$  and  $y$  are aliased at program point  $n$  is represented by an unordered pair  $\langle x, y \rangle$  at  $n$ . The encoding of **calling context** is the set of **reaching aliases (RAs)** that exists at entry of procedure  $p$  containing  $n$  when  $p$  is invoked from a particular call site.

	reaching alias
<pre> int *p, q, r; void main () { </pre>	
<pre>     p = &amp;q; n1 :  A (); </pre>	<pre> { [ϕ, ⟨*p, q⟩] } { [ϕ, ⟨*p, q⟩] } </pre>
<pre>     p = &amp;r; n2 :  A (); } </pre>	<pre> { [ϕ, ⟨*p, r⟩] } { [ϕ, ⟨*p, r⟩] } </pre>
<pre> void A () { </pre>	<pre> { [⟨*p, q⟩, ⟨*p, q⟩], [⟨*p, r⟩, ⟨*p, r⟩] } </pre>
<pre> n3 :  B (); } </pre>	<pre> { [⟨*p, q⟩, ⟨*p, q⟩], [⟨*p, r⟩, ⟨*p, r⟩] } </pre>
<pre> void B () { } </pre>	<pre> { [⟨*p, q⟩, ⟨*p, q⟩], [⟨*p, r⟩, ⟨*p, r⟩] } </pre>

# Interprocedural Side-Effect Analysis

## Assumptions:

- Simple programs
- No setjmp and longjmp
- “By-reference” passing: pointers

# Example

```
int x, y, k;
R(int *b)
{
    if (*b)
        { b = &k;
          *b = 0; }
    (*b)++
}

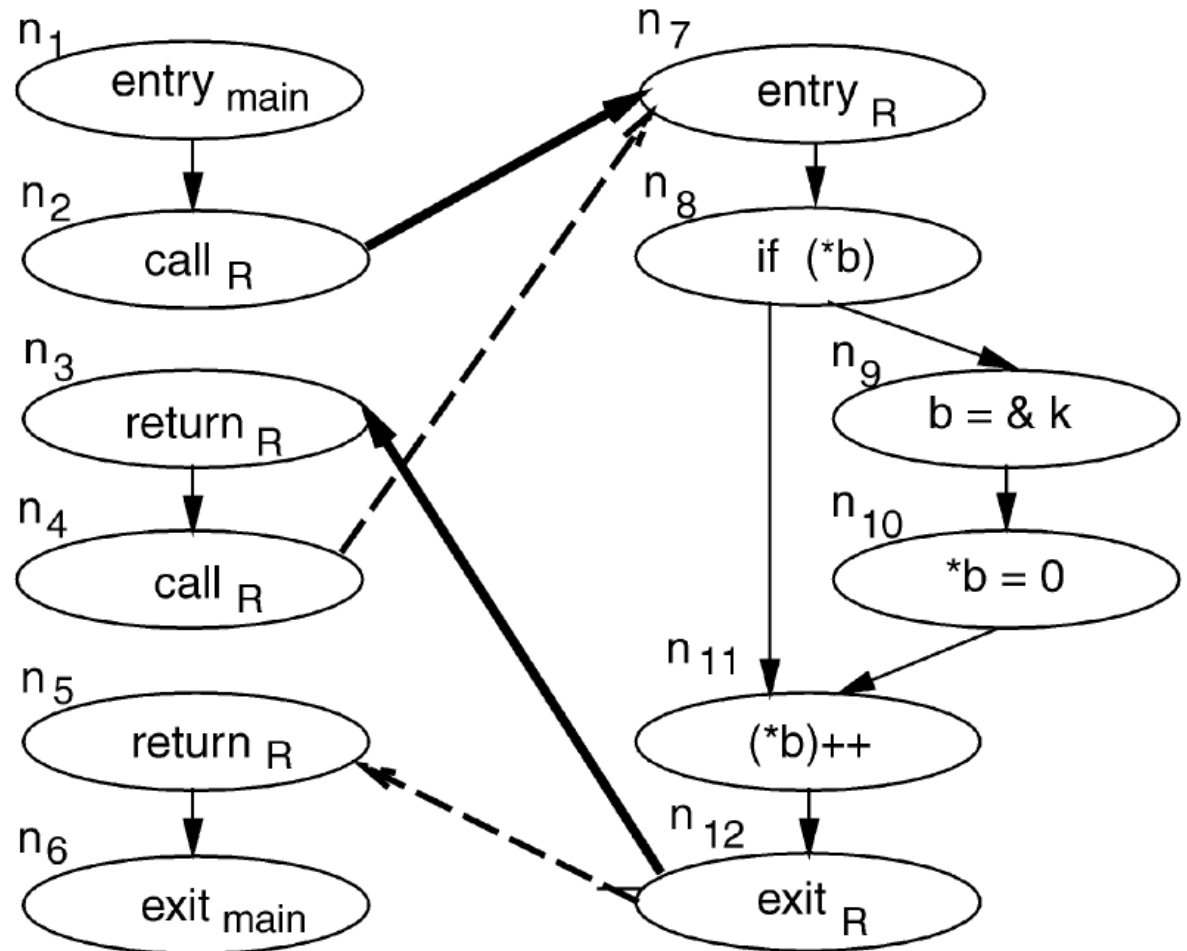
main()
{
    R(&x);
    R(&y);
}
```



# Example

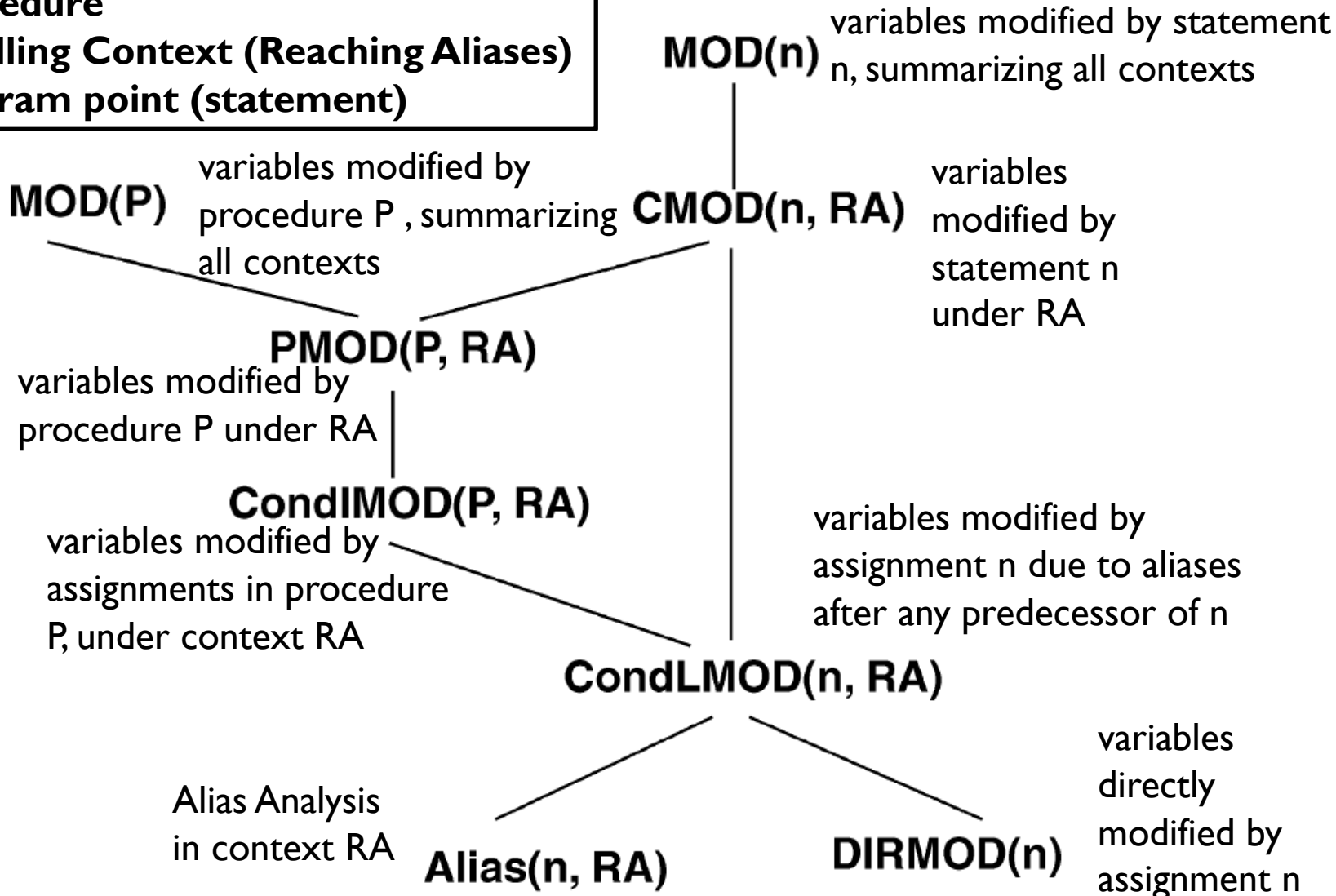
```
int x, y, k;
R(int *b)
{
  if (*b)
  { b = &k;
    *b = 0; }
  (*b)++
}

main()
{
  R(&x);
  R(&y);
}
```



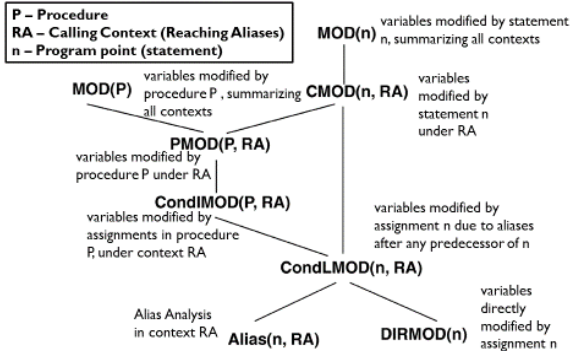
# Decomposition of the Analysis MOD(n) and MOD(P)

**P – Procedure**  
**RA – Calling Context (Reaching Aliases)**  
**n – Program point (statement)**



# Example

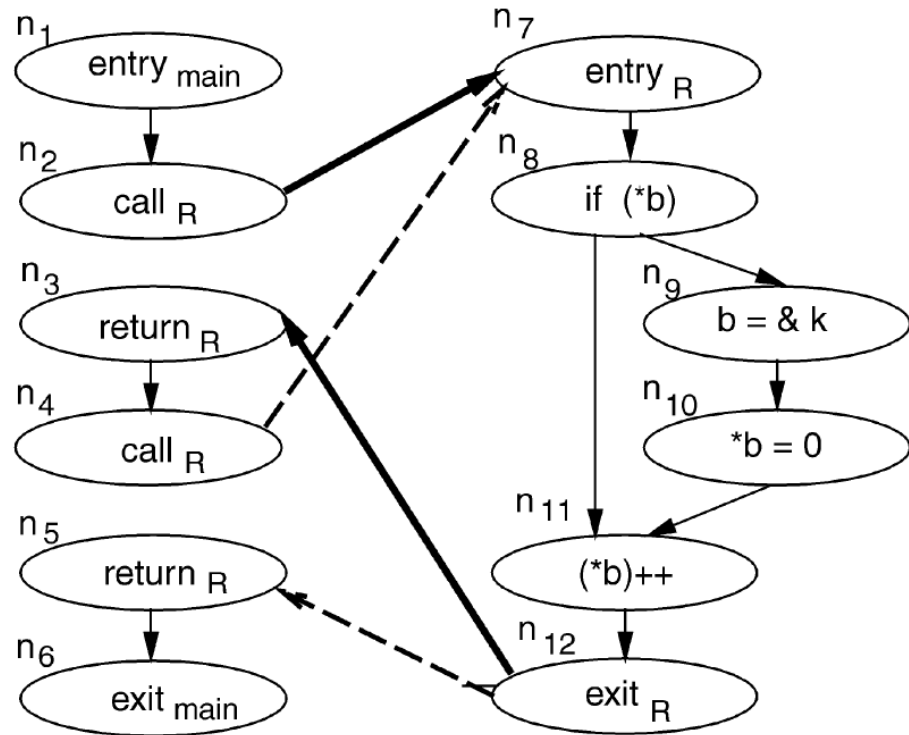
## Decomposition of the Analysis MOD(n) and MOD(P)



```

int x, y, k;
R(int *b)
{
  if (*b)
  { b = &k;
    *b = 0; }
  (*b)++
}

main()
{
  R(&x);
  R(&y);
}
    
```

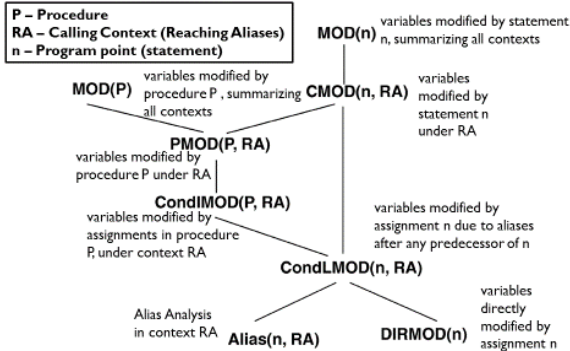


Reaching Alias	Alias Solutions for R					
	<i>n</i> <sub>7</sub>	<i>n</i> <sub>8</sub>	<i>n</i> <sub>9</sub>	<i>n</i> <sub>10</sub>	<i>n</i> <sub>11</sub>	<i>n</i> <sub>12</sub>
$\phi$			<*b,k>	<*b,k>	<*b,k>	<*b,k>
<*b,x>	<*b,x>	<*b,x>			<*b,x>	<*b,x>
<*b,y>	<*b,y>	<*b,y>			<*b,y>	<*b,y>

^ Global variables in C are initialized to zero  
 ^^ Flow sensitive analysis results

# Example

## Decomposition of the Analysis MOD(n) and MOD(P)

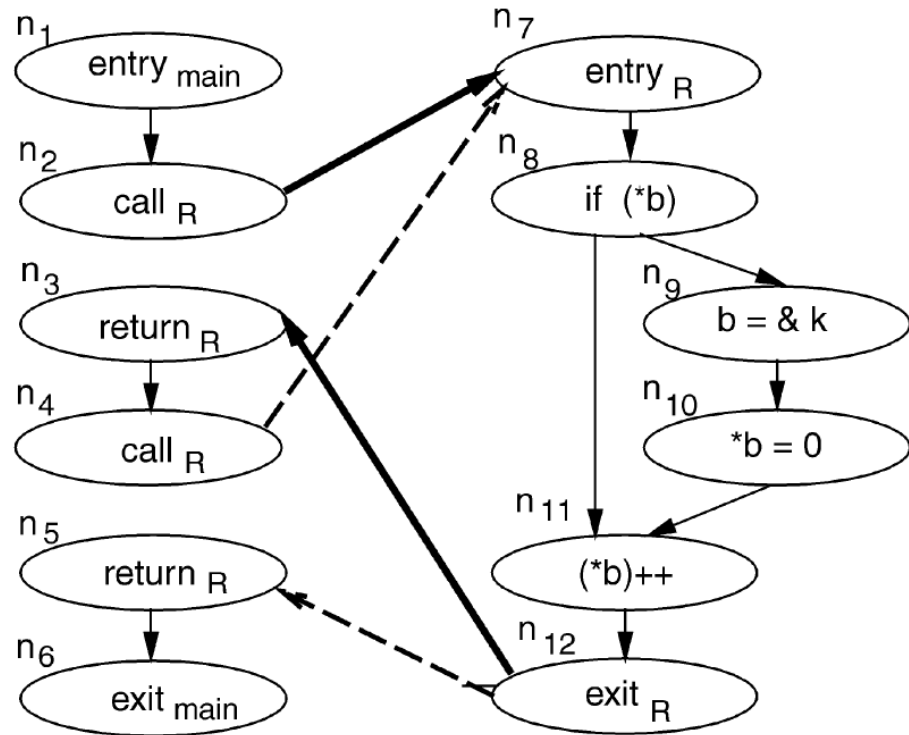


```

int x, y, k;
R(int *b)
{
  if (*b)
  { b = &k;
    *b = 0; }
  (*b)++
}

main()
{
  R(&x);
  R(&y);
}

```



Reaching Alias	<i>PMOD</i> Solutions for <i>main</i>
$\phi$	{ x, k, y }

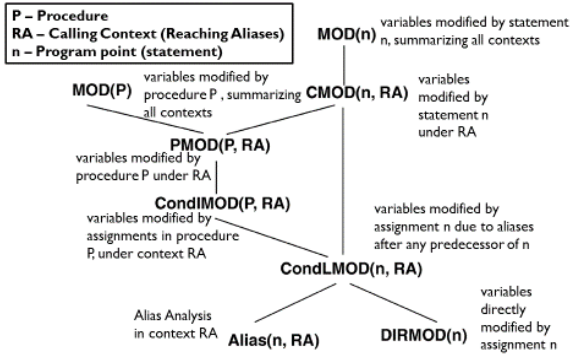
Reaching Alias	<i>PMOD</i> Solutions for R
$\phi$	{ k, b }
<*b,x>	{ x }
<*b,y>	{ y }

Reaching Alias	<i>CMOD</i> Solutions for <i>main</i>					
	<i>n</i> <sub>1</sub>	<i>n</i> <sub>2</sub>	<i>n</i> <sub>3</sub>	<i>n</i> <sub>4</sub>	<i>n</i> <sub>5</sub>	<i>n</i> <sub>6</sub>
$\phi$		{ x, k }		{ y, k }		

Reaching Alias	<i>CMOD</i> Solutions for R					
	<i>n</i> <sub>7</sub>	<i>n</i> <sub>8</sub>	<i>n</i> <sub>9</sub>	<i>n</i> <sub>10</sub>	<i>n</i> <sub>11</sub>	<i>n</i> <sub>12</sub>
$\phi$			{ b }	{ k }	{ k }	
<*b,x>					{ x }	
<*b,y>					{ y }	

# Example

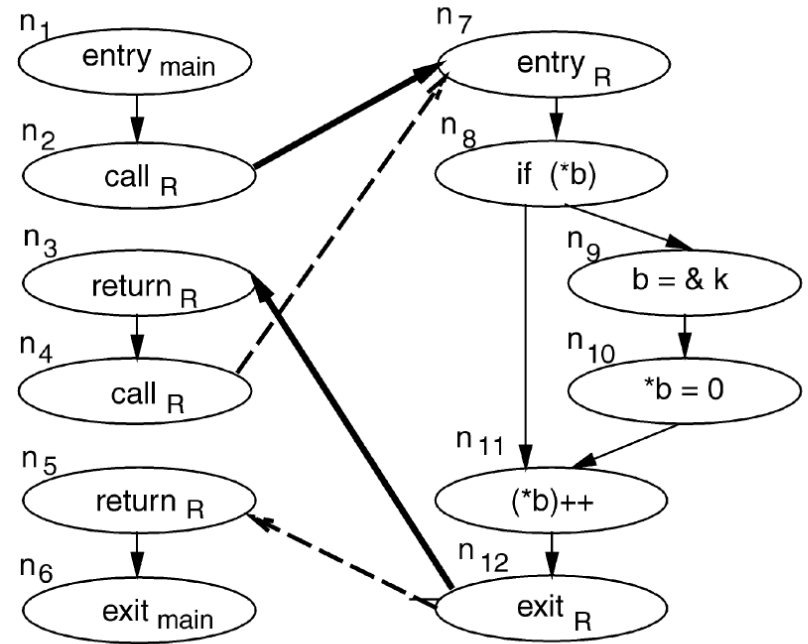
## Decomposition of the Analysis MOD(n) and MOD(P)



```

int x, y, k;
R(int *b)
{
  if (*b)
  { b = &k;
    *b = 0; }
  (*b)++
}

main()
{
  R(&x);
  R(&y);
}
  
```



### *FI*Alias solution for entire program

<*b,k>
<*b,x>
<*b,y>

<i>PMOD</i> Solution for main	<i>PMOD</i> Solution for R
{ x, y, k }	{ x, y, k, b }

<i>CMOD</i> Solutions for main						<i>CMOD</i> Solutions for R					
$n_1$	$n_2$	$n_3$	$n_4$	$n_5$	$n_6$	$n_7$	$n_8$	$n_9$	$n_{10}$	$n_{11}$	$n_{12}$
	{k, x, y }		{k, x, y }					{ b }	{ k, x, y }	{ k, x, y }	

Fig. 13.  $MOD_C(FI\text{Alias})$  solution for the example program of Figure 11.

# Interprocedural Side-Effect Analysis

## From Local Analysis:

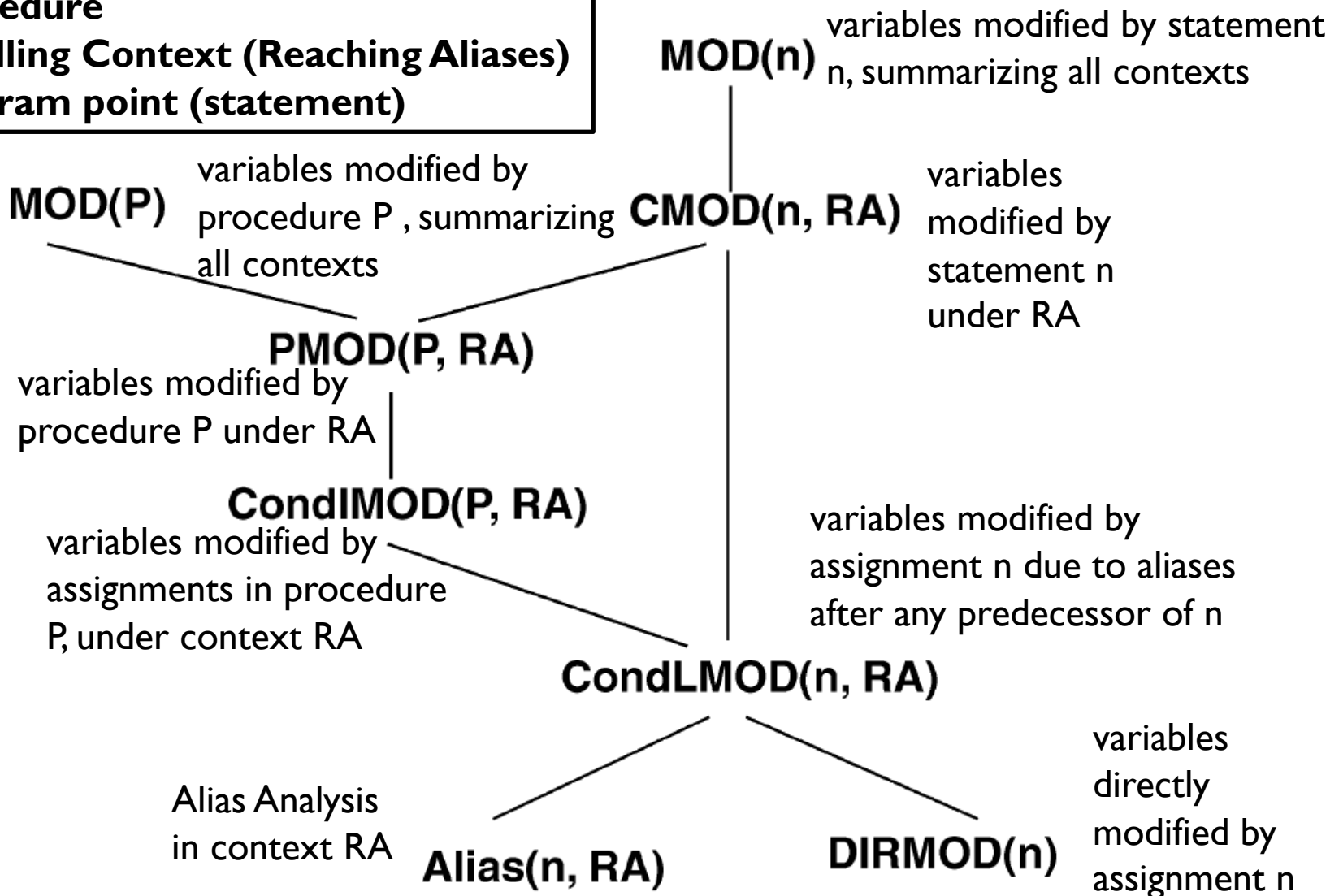
- **DIRMOD(s)**: variables directly modified by assignment  $s$  (no need for dataflow analysis)
- **$B_C(\text{VarSet})$** : Translates VarSet from names in callee (F) to names in caller at call-site C

IP dataflow problem is decomposed into several dataflow equations. They are solved by iteration on the call graph.

# Decomposition of the Analysis

## MOD(n) and MOD(P)

**P – Procedure**  
**RA – Calling Context (Reaching Aliases)**  
**n – Program point (statement)**



# Interprocedural Side-Effect Analysis

## CondLMOD( $n$ , RA):

variables modified by assignment  $n$  due to aliases after any predecessor of  $n$ , under context RA

includes trivial aliases  $\langle *p, *p \rangle$  for every location.

$$\text{CondLMOD}(n, RA) = \bigcup_{p:p \rightarrow n} \left\{ X_1 \mid \begin{array}{l} (X_1, X_2) \in \text{Alias}(p, RA) \\ \wedge X_2 = \text{DIRMOD}(n) \end{array} \right\}$$

## CondIMOD( $P$ , RA):

variables modified by assignments in procedure  $P$ , under RA

$$\text{CondIMOD}(P, RA) = \bigcup_{\text{assignments } n \in P} \text{CondLMOD}(n, RA)$$



# Interprocedural Side-Effect Analysis

## PMOD(P,RA):

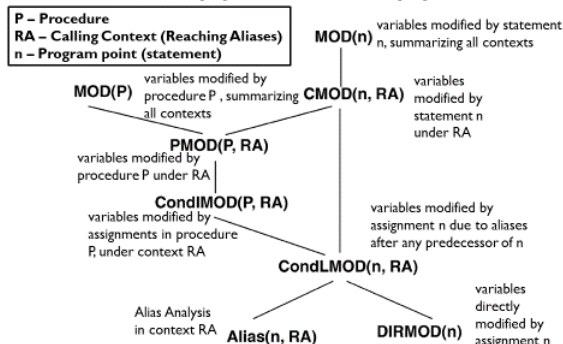
variables modified by procedure P under RA

$$\text{PMOD}(P, RA) = \text{CondIMOD}(P, RA) \cup \bigcup_{C_Q \in P} b_{C_Q}(\text{PMOD}(Q, RA'))$$

$C_Q \in P$  : call to  $Q$

$RA' \in \text{contexts\_of}(C_Q, RA)$

### Decomposition of the Analysis MOD(n) and MOD(P)



# Interprocedural Side-Effect Analysis

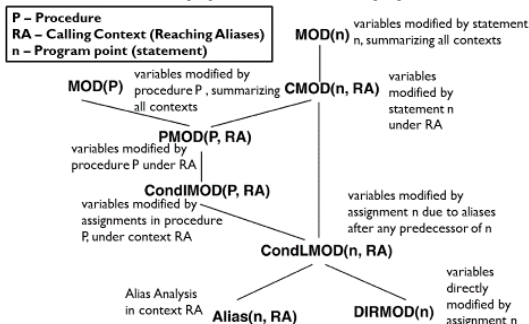
## CMOD(n,RA):

variables modified by statement  $n$  under  $RA$

$$CMOD(n, RA) = \begin{cases} CondLMOD(n, RA) & \text{if } n \text{ is an assignment} \\ \bigcup_{RA' \in contexts\_of(n, RA)} b_n(PMOD(Q, RA')) & \text{if } n \text{ is a call to } Q \\ \phi & \text{otherwise} \end{cases}$$

### Decomposition of the Analysis

#### MOD(n) and MOD(P)



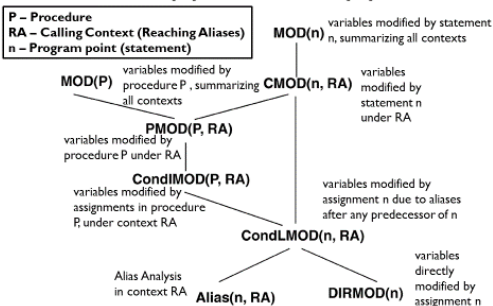
# Interprocedural Side-Effect Analysis

Finally:

$$\text{MOD}(n) = \bigcup_{\text{all contexts } RA \text{ for } P} \text{CMOD}(n, RA)$$

$$\text{MOD}(P) = \bigcup_{\text{all contexts } RA \text{ for } P} \text{PMOD}(P, RA)$$

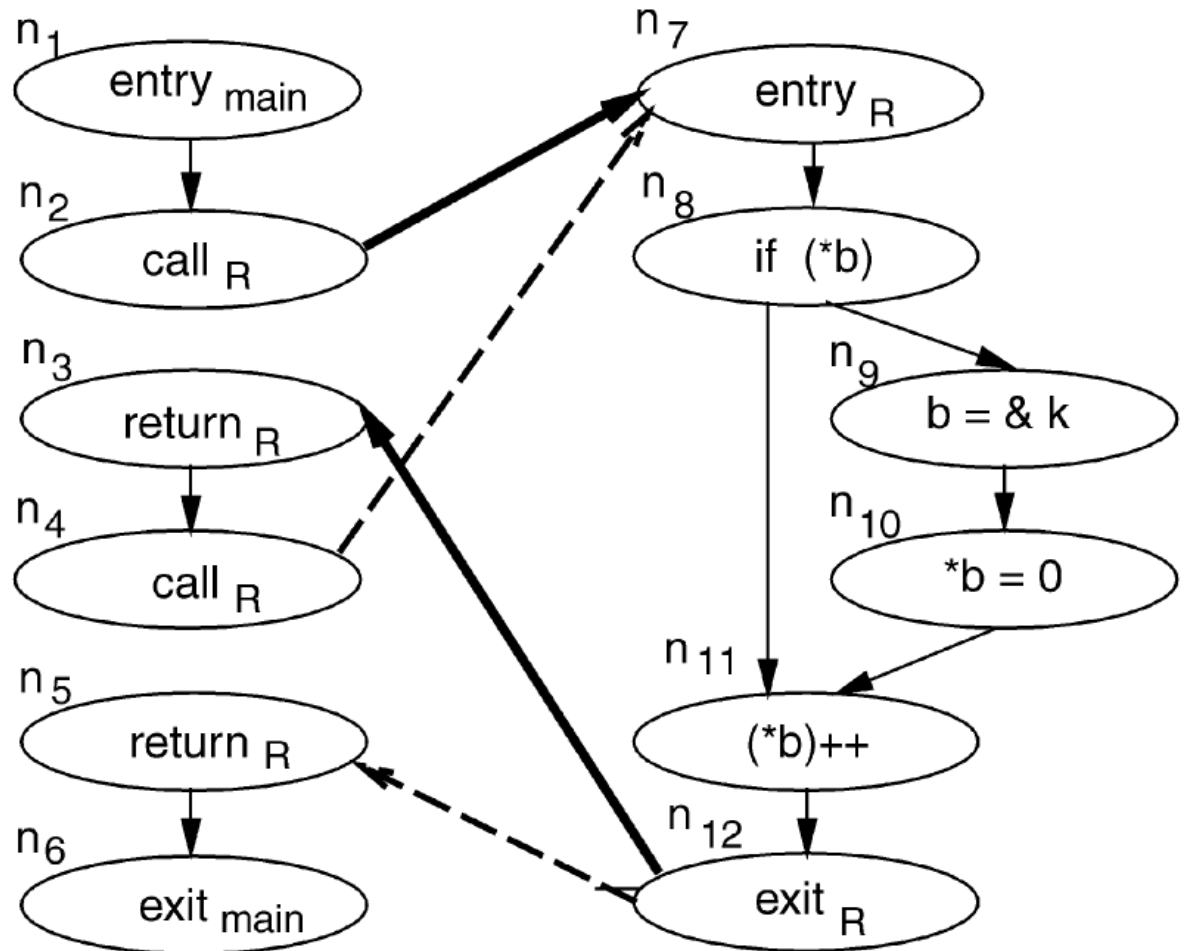
## Decomposition of the Analysis MOD(n) and MOD(P)



# Example

```
int x, y, k;
R(int *b)
{
  if (*b)
  { b = &k;
    *b = 0; }
  (*b)++
}

main()
{
  R(&x);
  R(&y);
}
```



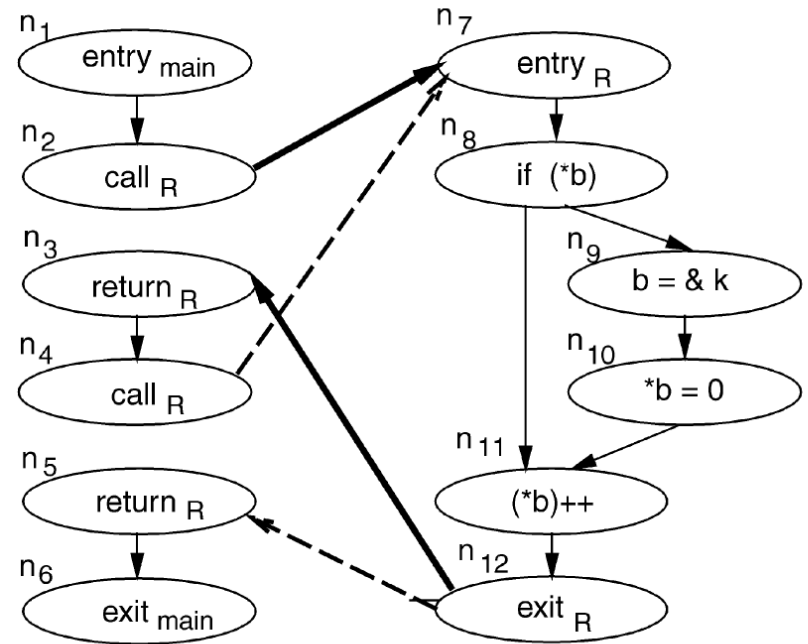
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  R(&y);
}

```



Reaching Alias	Alias Solutions for R					
	$n_7$	$n_8$	$n_9$	$n_{10}$	$n_{11}$	$n_{12}$
$\phi$			$\langle *b, k \rangle$	$\langle *b, k \rangle$	$\langle *b, k \rangle$	$\langle *b, k \rangle$
$\langle *b, x \rangle$	$\langle *b, x \rangle$	$\langle *b, x \rangle$			$\langle *b, x \rangle$	$\langle *b, x \rangle$
$\langle *b, y \rangle$	$\langle *b, y \rangle$	$\langle *b, y \rangle$			$\langle *b, y \rangle$	$\langle *b, y \rangle$

Reaching Alias	<i>PMOD</i> Solutions for <i>main</i>
$\phi$	{ x, k, y }

Reaching Alias	<i>PMOD</i> Solutions for R
$\phi$	{ k, b }
$\langle *b, x \rangle$	{ x }
$\langle *b, y \rangle$	{ y }

Reaching Alias	<i>CMOD</i> Solutions for <i>main</i>					
	$n_1$	$n_2$	$n_3$	$n_4$	$n_5$	$n_6$
$\phi$		{ x, k }		{ y, k }		

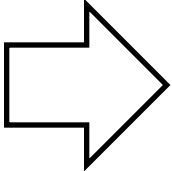
Reaching Alias	<i>CMOD</i> Solutions for R					
	$n_7$	$n_8$	$n_9$	$n_{10}$	$n_{11}$	$n_{12}$
$\phi$			{ b }	{ k }	{ k }	
$\langle *b, x \rangle$					{ x }	
$\langle *b, y \rangle$					{ y }	

# **INTERPROCEDURAL OPTIMIZATIONS**

# Inline Substitution

The code from one subroutine is substituted at the call site; formal parameters are replaced by actual parameters:

```
int f (int x) {  
    int r = g(x);  
    return r; }  
int g(int y) {  
    return 2*y}
```



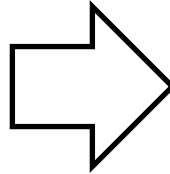
```
int f (int x) {  
    int r = 2*x;  
    return r;  
}
```

- Can always be applied
- But can be too expensive (exponential blowup)
- Recompile of a single function will cause project recompilation

# Function Cloning

Specialize function for specific values of the parameters

```
int f(int a[], int s) {  
    for (i=0;i<len(a);i++)  
        a[i*s-s+1]=  
            a[i*s-s+1]+3;  
}
```



```
int f_s1(int a[], int s) {  
    for (i=0;i<len(a);i++)  
        a[i*s-s+1]=a[i*s-s+1]+3;  
}
```

**Vectorizable when  $s > 0$ ,**  
**not vectorizable when  $s = 0$**

```
int f_s0(int a[], int s) {  
    for (i=0;i<len(a);i++)  
        a[1]=a[1]+3;  
}
```

- Enhances the applicability of constant propagation



# Separate Compilation

## The problem

Interprocedural data flow analysis introduces subtle dependences

- optimized procedures are program-specific
- correctness of object code depends on whole program

Changing one procedure can force many compilations:

- the procedure, itself, for different programs
- other procedures within those programs

## Solution: Separate Compilation

- Allows subsets of a program to be compiled separately and then linked together into a final executable.
- After a module is changed, only need to re-do selected optimizations on selected procedures
- Analysis to determine which files were changed: **dataflow!**